

## INERTIAL NORTH FINDER

### FIELD AND BACKGROUND OF THE INVENTION

10       The present invention relates to direction finding, and, more particularly, to a method and apparatus for determining the orientation of a body, such as a vehicle or a theodolite, relative to a local coordinate system.

15       Many methods and devices are known for determining the geographic heading of a body such as a vehicle. A summary of North finding techniques can be found in chapter 9 of "Strapdown inertial navigation technology" by D.H. Titterton and J.L. Weston, ISBN 0863412602, IEE Publishing, England. Magnetic compasses, which are among the oldest of such devices, find the direction of magnetic North, rather than geographic North, so their readings must be corrected for the local deviation of magnetic North from geographic North. More modern methods and 20      devices include gyrocompasses and methods based on signals received from external transmitters such as the GPS satellite network. Gyro-compassing performance (accuracy and duration) is very sensitive to a gyroscope's drift. The process is very long, usually lasting between 10 minutes and 40 minutes. For high accuracy, a very expensive gyroscope must be used. The methods based on external signals are, by 25      definition, not autonomous.

30       Methods and devices using accelerometers for determining the geographic heading of a body are also known. They include US Patent No. 6,502,055 to Reiner et al. and the references cited therein, in particular the paper by Sun et al., "Accelerometer based North finding system", IEEE, Mar. 13-16, 2000. Sun et al. use one or more linear accelerometers to find North. Sun's and similar systems based on linear accelerometers suffer from two main disadvantages:

- a) all linear accelerometers measure linear vibration in addition to Coriolis acceleration. The magnitude of a Coriolis acceleration due to earth rotation is no more

than 150-200  $\mu\text{G}$ . Identification of this acceleration is too difficult on the background of a typical field linear vibration (10-50 mG).

b) use of a system such as Sun's is possible only in a vertical position of the rotative axis, because a tilt of the accelerometer rotative base coupled with the 5 accelerometer residual misalignment provide a disturbance, which induces a non-separable error to the azimuth measurement.

In contrast with all accelerometer-based prior art North finding systems that use linear accelerometers, the system of the present invention uses an angular accelerometer, specifically a fluid rotor angular accelerometer. An angular 10 accelerometer is a single axis non-gyroscopic device, which provides an electrical signal proportional to angular acceleration. Angular accelerometers that use the fluid rotor concept shown in FIG. 1 are known in the art, described for example in section 6.6.1, chapter 6 of Titterton and Weston above, and manufactured for example by Columbia Research Laboratories, Inc 1925 Mac Dade Blvd. Woodlyn, Pa. 19094, or 15 Jewell Instruments LLC, 850 Perimeter Road, Manchester, NH 03103, USA. FIG. 1 shows a fluid containing toroidal vessel 10 that rotates clockwise around a central symmetry axis 12, which is perpendicular to (coming out of) the plane of the page. Vessel 10 is defined by an internal diameter 14, a mean radius R and an external 20 diameter 18. Toroidal vessel 10 includes a sensing element, preferably a piezo-deflection element, most preferably a piezo-ceramic transducer membrane 20, for transducing the fluid pressure into an electrical signal. When static, membrane 20 is parallel to a radial direction 22. When deflected by an inertial force  $F_i$ , membrane 20 produces an electrical output. If only the alternating component of angular 25 acceleration is needed for the measurement, the piezo-ceramic membrane pickoff can be used for measuring angular acceleration. Such fluid rotor accelerometers are advantageous in that a homogeneous non-compressible fluid provides ruggedness under linear vibration and acceleration.

In terms of principle of operation, the angular acceleration (out of plane)  $\dot{\omega}$  of a fluid of mass "m" positioned on a toroidal vessel at a mean radius R is related to 30 the inertial force  $F_i$  applied to the piezo-ceramic membrane by

$$F_i = mR\dot{\omega} \quad (1)$$

The electrical output of the device is:

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$$U_{out} = k_{piezo} m R \dot{\omega} \quad (2)$$

where  $k_{piezo}$  is the piezo-ceramic transducer scale factor.

In view of the disadvantages existing in prior art linear accelerometer-based direction finders, there is a widely recognized need for, and it would be highly 10 advantageous to have, a North finding seeker that does not use linear accelerometers with their attendant disadvantages.

#### SUMMARY OF THE INVENTION

15 According to the present invention there is provided a non-gyroscopic inertial seeker system for determining the azimuth of a body relative to the true North direction, comprising a fluid rotor angular accelerometer positioned on and revolving on the body, the accelerometer providing a periodic output signal, and means to extract from the periodic output signal the body azimuthal direction relative to the 20 true North direction.

According to the present invention there is provided a method for determining the azimuth of a body relative to the true North direction, comprising steps of providing a fluid rotor angular accelerometer, the accelerometer including at least one Coriolis force sensing element, rotating the angular accelerometer relative to the body 25 to provide a periodic output signal correlated with a body direction, and using the periodic output signal to determine the azimuth of said body direction relative to the true North direction.

#### BRIEF DESCRIPTION OF THE DRAWINGS

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The invention is herein described, by way of example only, with reference to the accompanying drawings, wherein:

FIG. 1 is a schematic description of the fluid rotor angular accelerometer concept;

FIG. 2 is a schematic description of Coriolis force measurement using a toroidal fluid rotor angular accelerometer;

5 FIG. 3 shows schematically a preferred embodiment of the system for North seeking of the present invention;

FIG. 4 shows the output of the angular accelerometer and synchronization pulse;

10 DESCRIPTION OF THE PREFERRED EMBODIMENTS

The present invention is of a non-gyroscopic inertial North seeker system, and of a method for finding North. Specifically, the present invention is of a system and method for finding North based on the measurement of the Coriolis effect in a fluid 15 rotor angular accelerometer.

The principles and operation of a North seeker based on a fluid rotor angular accelerometer according to the present invention may be better understood with reference to the drawings and the accompanying description.

Referring now to the drawings, FIG. 2 shows schematically a Coriolis force 20 acceleration measurement using a toroidal fluid rotor angular accelerometer. The figure shows a toroidal fluid rotor angular accelerometer 40 similar to accelerometer 20 of FIG. 1 which includes a sensing element 42. As in FIG. 1, sensing element 42 is preferably a piezo-ceramic membrane. Let us look at an elementary mass  $m_n$  placed at a radius  $r_n$  in the torus, which is now rotated around a vertical axis 44 (lying in the 25 plane of the paper) with a velocity  $\omega$ . The mass feels a Coriolis acceleration  $a_c$ .

$$\overline{a}_c = 2 \overline{\Omega} \times \overline{V}_n$$

$$a_c = 2\Omega\omega r_n; F_n = 2\Omega m_n \omega r_n \quad (3)$$

30 where  $V_n$  is the linear velocity of  $m_n$ , produced by its rotation on radius  $r_n$ ,  $F_n$  is the elementary Coriolis force, and  $\Omega$  is the inertial angular velocity on an axis perpendicular to axis 44. The integral Coriolis force applied to the piezo-ceramic

membrane  $F_c$  is then given by the integration of all masses over a quarter torus (e.g. over the angle  $\varphi$  between 0 and  $90^\circ$ )

$$\begin{aligned} F_c &= 4\Omega \omega \int_0^{\pi/2} \rho S R^2 \varphi \sin^2 \varphi d\varphi; \\ F_c &= 4\Omega \omega \rho S R^2 \int_0^{\pi/2} \varphi \sin^2 \varphi d\varphi; \end{aligned} \quad (4)$$

5 where  $\rho$  is the fluid density,  $R$  is the torus mean radius,  $S$  is the torus cross-section.

- FIG. 3 shows schematically a preferred embodiment of a system 50 for North seeking of the present invention. System 50 includes a toroidal fluid rotor angular accelerometer 52 located on a body 54. The earth coordinates are given by an orthogonal axis set (X, Y, Z), with "Local Vertical" being Z, and true North being X.
- 10 The body is defined by a body coordinate system, which in this case consists of orthogonal axes X', Y', Z'. The accelerometer is defined by an accelerometer coordinate system, which in this case consists of orthogonal axes X'', Y'', Z''. Body 54 seeks to find a body azimuthal direction 62 vs. the geographical North direction 60. This azimuthal position is defined by an angle  $\psi$  between body direction (axis X') 62
- 15 and North direction (axis X) 60. In general, the body and the accelerometer (torus) local coordinate systems do not overlap. Thus, while the vertical (Z, Z', Z'') axes overlap as shown, the other two orthogonal axes of body and torus do not do so (except once every rotation, as explained below). As in FIGS. 1 and 2, accelerometer 52 includes one sensing element 66, which is preferably a piezo-ceramic membrane.
- 20 Optionally, accelerometer 52 may include a second piezo-ceramic membrane 68. The positioning of each membrane is identical with that described in FIG. 2.

As in FIG. 2, the accelerometer (torus) is rotated around a vertical (in the plane of the paper) axis 70 (which coincides with Z) with an angular velocity  $\omega$  relative to the body. Since both the body and the accelerometer are located on earth,

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$$\Omega = \Omega_h \cos(\omega t + \Psi)$$

where  $\Omega_h = |\Omega_{\text{earth}}| \cos \lambda$  is the horizontal component of the earth rate,  $\lambda$  is the latitude, and  $\psi$  is body azimuth position. Membrane 66 now experiences a Coriolis force  $F_c$  from the combined contributions of torus and earth rotations:

$$\dot{F}_c = 4(\Omega_h \cos(\omega t + \Psi)) \omega \rho S R^2 \int_0^{\pi/2} \varphi \sin^2 \varphi d\varphi \quad (5)$$

5 or

$$F_c = \Omega_h \pi \omega \rho S R^2 \cos(\omega t + \Psi) \quad (6)$$

As indicated by equation 6,  $F_c$  is periodic (sinusoidal). This is shown in FIG. 3 by arrows 72 of changing length.  $F_c$  is positive (upwards) for half a rotation cycle (180 degrees) and negative (downwards) for the other half. The deflection of the piezo-ceramic membrane caused by  $F_c$  is transduced by known means into a periodic electrical output voltage  $U_{out}$

$$U_{out} = k_{piezo} \Omega_h \pi \omega \rho S R^2 \cos(\omega t + \Psi) \quad (7)$$

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where  $k_{piezo}$  is a transducing factor.

The relative azimuthal position vs North is extracted from  $U_{out}$ . The means to extract the position include synchronization means in the form of a "zero" marker encoder 80 connected to system 50. Encoder 80 provides one pulse per full 360° revolution of the torus in body coordinates. The encoder produces this synchronization pulse when the body direction X' coincides with the torus direction X". An example of such an encoder may be a light source and a light detector positioned relative to the torus in such a way that a marker on the rotating torus cuts a light signal transmitted between the source and detector once every full 360° revolution.

The periodic electrical signal from the rotative base piezo-ceramic membranes are amplified by a charge amplifier and transmitted through means such as brushless slip-rings to the static body. This signal is sampled many times a revolution and over a large number of revolutions, and acquired together with a synchronization pulse provided by encoder 80. After acquisition, this periodic signal is filtered by averaging over a large number of complete revolutions. The following Fourier series may now express the output of the accelerometer, using the synchronization and periodic signals:

(8)

$$\text{For } t=0: \quad U_{\text{out}} = A_0 + A_1 \sin(\omega \cdot n/f_{\text{samp}}) + B_1 \cos(\omega \cdot n/f_{\text{samp}})$$

where  $n$  is the sampling serial number, and  $f_{\text{samp}}$  is the sampling frequency. Since  
5  $\sin(x)$  and  $\cos(x)$  are synchronized with the pulse signal provided by the zero encoder,  
the value of the Fourier coefficients  $A_0$ ,  $A_1$  and  $B_1$  can be determined by a fit of the  
data points in FIG. 4, preferably by a least squares method. The relative North angle is  
then given by

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$$\psi = \arctg \left( \frac{A_1}{B_1} \right) \quad (9)$$

All publications, patents and patent applications mentioned in this specification  
are herein incorporated in their entirety by reference into the specification, to the same  
extent as if each individual publication, patent or patent application was specifically  
and individually indicated to be incorporated herein by reference. In addition, citation  
or identification of any reference in this application shall not be construed as an  
admission that such reference is available as prior art to the present invention.

15 While the invention has been described with respect to a limited number of  
embodiments, it will be appreciated that many variations, modifications and other  
applications of the invention may be made.